Maclaurin Series of $\sin x$

The Maclaurin series of $\sin x$ is

$$\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \cdots$$

It can be shown that the series converges for all values of x.

We can use this series to estimate numerically the values of $\sin x$. For example, we have

$$\sin(0.5) \approx (0.5) - \frac{(0.5)^3}{3!} + \frac{(0.5)^5}{5!} \approx 0.4794.$$

You can check this with your calculator but be sure to set it in radians.

The following graphs illustrate graphically the fact that adding more terms from the Maclaurin series improves the approximation.



Gilles Cazelais. Typeset with IATEX on January 31, 2007.